

Energy Levels and Crystal-Field Calculations of Europium and Terbium in Yttrium Aluminum Garnet*

J. A. KONINGSTEIN

Bell Telephone Laboratories, Murray Hill, New Jersey

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Experimental and theoretical studies of the trivalent europium and terbium ions in yttrium aluminum garnet are reported in this communication. From crystal-field calculations on the split 7F manifolds of Eu^{3+} and Tb^{3+} , it is concluded that the crystal field is approximately tetragonal. Agreement between experimental and calculated splitting patterns is satisfactory for those Stark components of 7F manifolds which are not far removed from the center of gravity.

I. INTRODUCTION

ENERGY levels of some rare-earth ions in yttrium aluminum garnet (YAlG) and yttrium gallium garnet (YGaG) are reported in the literature.¹⁻⁶ The splitting of J manifolds of Er^{3+} :YGaG has been explained by Pappalardo⁴ on the basis of a crystal field of cubic symmetry. The crystallographic data of Geller and Gilleo⁷ on the position of ions in YIG indicate that yttrium ions (which are replaced by rare-earth ions) occupy sites of orthorhombic symmetry. Dillon and Walker⁸ have calculated the crystal field for this site. Recent calculations on the split manifolds of Nd^{3+} :YAlG indicate⁶ that the symmetry of the crystal field is approximately tetragonal. In this communication the energy level diagrams of Eu^{3+} and Tb^{3+} :YAlG are discussed. The crystal-field calculations indicate that a slight deviation occurs from tetragonal symmetry. This deviation has been found to be larger in the gallium garnet than in the aluminum garnet.

II. EXPERIMENTAL

Absorption spectra of samples containing ~ 5 – 10% Eu^{3+} and Tb^{3+} :YAlG have been studied in the infrared with a Beckman IR7 spectrometer. In the visible, a $\frac{1}{2}$ -m Jarrell-Ash spectrometer was used. The fluorescence spectrum of Eu^{3+} :YAlG and Tb^{3+} :YAlG was also studied, and the fluorescence was excited with a filtered high-pressure Hg light source. The absorption and fluorescence spectra of these materials were studied at 30, 77, and 300°K.

1. Absorption Spectrum of Eu^{3+} : YAlG

The energy level diagram of the trivalent europium ion is now well known⁹ for J states up to 28 000 cm^{-1} .

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¹ R. Pappalardo and D. L. Wood, *J. Chem. Phys.* **33**, 1734 (1960).

² D. L. Wood, *J. Chem. Phys.* **39**, 1671 (1963).

³ L. G. Van Uitert, R. C. Linares, and A. A. Ballman, *J. Chem. Phys.* **36**, 702 (1962).

⁴ R. Pappalardo, *Z. Physik* **173**, 374–391 (1963).

⁵ R. Pappalardo, *Nuovo Cimento* **26**, 4, 748 (1962).

⁶ J. A. Koningstein and J. E. Geusic, preceding paper, *Phys. Rev.* **135**, A711 (1964).

⁷ S. Geller and M. A. Gilleo, *Phys. Chem. Solids* **3**, 30 (1957).

⁸ J. F. Dillon and L. R. Walker, *Phys. Rev.* **124**, 1401 (1961).

⁹ G. H. Dieke and H. M. Crosswhite, *Appl. Optics* **2**, 7, 675 (1963).

The 7F_1 state has been established at $\sim 350 \text{ cm}^{-1}$ above the ground state 7F_0 . The transitions in the absorption spectrum at room temperature for Eu^{3+} :YAlG originates in levels of the 7F_0 and 7F_1 manifolds.

a. Absorption Spectrum in the Visible

The transition between the 7F_0 and 5D_0 states of Eu^{3+} :YAlG should occur at about $\sim 5810 \text{ \AA}$. No absorption has been found in that region; however, a triplet was recorded at 5905.5, 5912.5, and 5968.5 \AA (see Fig. 1). Upon cooling of the sample, this triplet disappeared, indicating that the transitions originate in excited levels. Fluorescence of Eu^{3+} : CdF_2 has been observed by Kingsley and Prener¹⁰ in the same part of the spectrum, and they attributed it to transitions between the 5D_0 and 7F_1 manifolds. The transitions of 7F_1 to 5D_0 for Eu^{3+} :YAlG occur apparently at the three wavelengths mentioned above.

Two rather strong absorptions have been detected at 5276.5 and 5265.0 \AA . The linewidth of these absorptions decreased on cooling to liquid N_2 temperature. These two bands represent transitions between the ground state and two of the Stark levels of the 5D_1 manifold. Other absorptions at 5345, 5350.8, and 5406.4 \AA disappeared when the sample was cooled to 77°K. Transitions between levels of the 7F_1 and 5D_1 manifolds of Eu^{3+} :YAlG occur in this region. Also transitions from a level $824 \pm 2 \text{ cm}^{-1}$ above the ground state to the levels of 5D_0 and 5D_1 manifolds have been observed (300°K) at 6099.0, 5513, and 5503 \AA . The absorption spectrum described up to this point enables one to set up a part of the term scheme of Eu^{3+} : $\text{Y}_3\text{Al}_2(\text{AlO}_4)_3$ (see Fig. 2). The position of the level of the 5D_0 state was calculated to be at $17\,220 \pm 5 \text{ cm}^{-1}$ above the ground state.

Transitions from the ground state and levels of the excited state 7F_1 to the crystal-field components of the 5D_2 and 5D_3 manifolds have been observed as weak absorptions between 4665 and 4045 \AA . The absorption bands in the visible are given in Table I.

b. Absorption Spectrum in the Infrared

Strong absorptions have been observed in the region from 1900 to 5400 cm^{-1} at room temperature and at

¹⁰ J. D. Kingsley and J. S. Prener, *Phys. Rev.* **126**, 458 (1962).

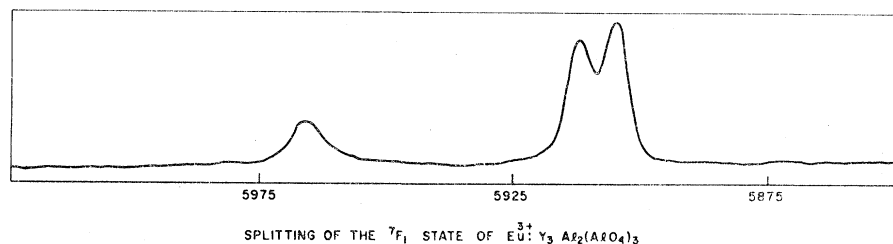


FIG. 1. The absorption spectrum of $\text{Eu}^{3+}:\text{YAIG}$ between 5975 and 5875 Å at 300°K.

~30°K. Strong host-lattice absorptions below 1900 cm^{-1} prevent the observation of transitions between the ground state and levels of the 7F_2 and 7F_1 manifolds. Four groups of absorptions have been found in the abovementioned spectral region. Transitions from the ground state to crystal-field components of the 7F_3 , 7F_4 , 7F_5 , and 7F_6 manifolds occur between 1916–1994 cm^{-1} ; 2863–3246 cm^{-1} ; 3791–4226 cm^{-1} , and 4976–5145 cm^{-1} . The part of the spectrum from 3.6–3.2 μ [2780–3230 cm^{-1}] and 2.1–1.8 μ [4760–5560 cm^{-1}] is shown in Figs. 3 and 4. The absorption spectrum of $\text{Eu}^{3+}:\text{YGa}_2(\text{GaO}_4)_3$ in the same spectral regions is also shown. A similarity between the two spectra exists, although the absorptions occur at somewhat different wavelengths. The spectra of $\text{Eu}^{3+}:\text{YAIG}$ and $\text{Eu}^{3+}:\text{YGaG}$ are quite similar and reveal the presence of doublets, the doublet separation in the gallium garnet being slightly larger than in the aluminum garnet. The infrared absorption bands of $\text{Eu}^{3+}:\text{YAIG}$ are listed in Table II.

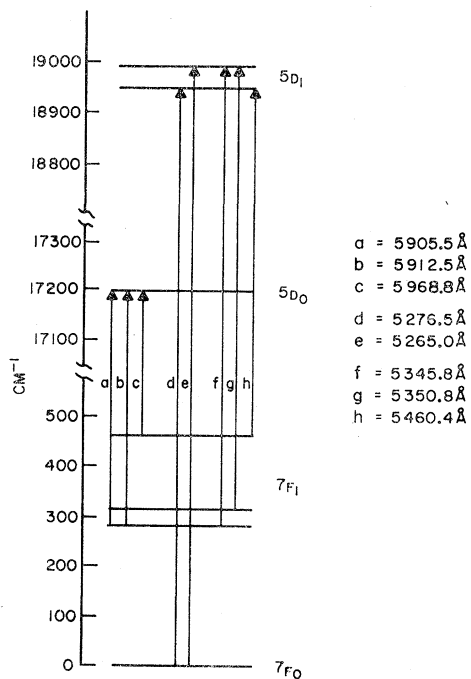


FIG. 2. Transitions of $\text{Eu}^{3+}:\text{YAIG}$ in the spectral region of 5975–5265 Å.

2. Fluorescence Spectrum of $\text{Eu}^{3+}:\text{YAIG}$

The fluorescence spectrum has been recorded at room temperature and 77°K in the spectral region of 5900 to 7110 Å. Strong fluorescence occurs at 5904.9, 5912.9, and 5964 Å, which originates in the level of the 5D_0 state and terminates on crystal field levels of the 7F_1 manifold. Other fluorescence lines have been recorded at 6097 and 6304 Å and at 6533.5, 6553.0, and 6567.0 Å. These fluorescence lines originate in the 5D_0 state and terminate on levels of the 7F_2 and 7F_3 manifolds. Additional high-resolution, low-temperature fluorescence measurements have been made available to us by Dr. D. L. Wood of this laboratory. A sharp but weak line at 17 211 cm^{-1} is assigned to the 5D_0 - 7F_0 transition. The position of 5D_0 state as obtained from the fluorescence measurement is to be compared with the absorption measurements in the visible at $17\,220 \pm 5 \text{ cm}^{-1}$ which was inferred from absorption measurements at room temperature (see Fig. 2). This apparent shift may be due to the fact that the fluorescence measurements were made at 77°K, while the absorption measurements were made at 300°K.

TABLE I. Absorption spectrum of $\text{Eu}^{3+}:\text{YAIG}$ from 6100–4050 Å.

300°K (Å)	Absorptions Intensity*	72°K (Å)	Assignment
6099.0	w	...	7F_2 - 5D_0
5968.8	m	...	
5912.5	st	...	7F_1 - 5D_0
5905.5	st	...	
5513	w	...	
5503	w	...	7F_2 - 5D_1
5406.4	m	...	
5350.8	m	...	7F_1 - 5D_0
5345.8	m	...	
5276.5	st	5276.4 (18 952 cm^{-1})	7F_0 - 5D_1
5265.0	st	5266.0 (18 991 cm^{-1})	
4746.8	w	...	
4727.3	w	...	7F_1 - 5D_2
4722.5	w	...	
4681.0	m	4681.5 (21 356 cm^{-1})	7F_0 - 5D_2
4661.0	m	4661.5 (21 448 cm^{-1})	
4655.8	m	4656.4 (21 473 cm^{-1})	
4120	vw	...	
4108	vw	...	7F_1 - 5D_3
4102	vw	...	
4097	vw	...	
4056	w	4058.5 (24 639 cm^{-1})	7F_0 - 5D_3
		4052.5 (24 678 cm^{-1})	
		4051.5 (24 683 cm^{-1})	
4049.0	w	4049.0 (24 697 cm^{-1})	

* w = weak; m = medium; st = strong; vw = very weak.

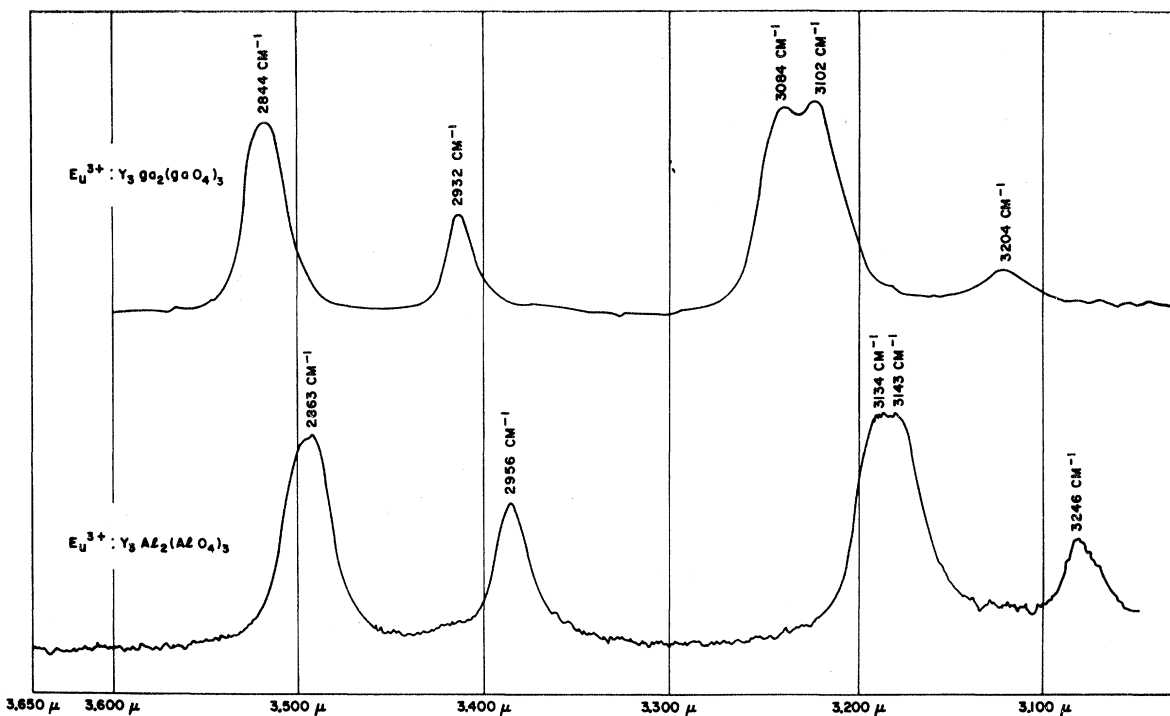


FIG. 3. The absorption spectrum of Eu^{3+} :YAlG and Eu^{3+} :YGaG between 3.6 and 3.1 μ at 30°K.

The fluorescence lines of Eu^{3+} :YAlG are listed in Table III.

3. Absorption Spectrum of Tb^{3+} : YAlG

The Tb^{3+} ion energy-level diagram is well known⁹ up to 28 000 cm^{-1} . The first excited state 7F_5 occurs at

$\sim 2000 \text{ cm}^{-1}$. The absorptions of Tb^{3+} : $\text{Y}_3\text{Al}_2(\text{AlO}_4)_3$ at 300°K or at lower temperatures originate from Stark levels of the 7F_6 manifold only.

TABLE II. The absorption spectrum of Eu^{3+} :YAlG in the infrared. Transitions originate in the 7F_0 level.

Absorptions (cm^{-1})	Intensity ^a	Assignment
1916	m	
1957	st	7F_3
1998	m	
2863	st	
2956	m	
3134	st	7F_4
3143	st	
3246	m	
3785	w	
3791	st	
3946	m	7F_5
4097	m	
4226	m	
4976	st	
4983	st	
5041	st	
5151	m	7F_6
5319	w	
5358	vw	
5445	vw	

^a The intensities are relative and valid inside A group only. w=weak; m=medium; st=strong; vw=very weak.

TABLE III. Fluorescence of Eu^{3+} :YAlG. All transitions originate in the level of 5D_0 .

Obs (Å)	Obs (300°K)	Obs (77°K)	Average (cm^{-1})	Infrared or visible absorption	Assignment
5904.9	5905.1	5912.8	16 934	286	
5912.4	5912.8	5912.8	16 913	307	7F_1
5964.8	5964.5	5964.5	16 766	454	455
6097.0	6096.8	6096.8	16 401	819	824
			6128 ^a	16 318	902
			6174 ^a	16 198	1022 ^b
6304.5	6304.0	6304.0	15 862	1358	...
			6498 ^a	15 389	1832
			6503 ^a	13 378	1842
6533.0	6534.0	6534.0	16 305	1915	1916
6553.0	6553.0	6553.0	15 259	1961	1957
			6571.0 ^a	15 218	2002
~6570			6574.0 ^a	15 212	2008
			6586.0 ^a	14 999	2221
			6961.8 ^a	14 364	2856
			6966.2 ^a	14 355	2863
			7011.1 ^a	14 263	2957
			7101.7 ^a	14 081	3139
7106.0	7107.3 ^a	7107.3 ^a	14 070	3150	3143
			7158.1 ^a	13 970	3250
			7444.3 ^a	13 433	3787
			8202.0 ^a	12 912	5028
			8225.0 ^a	12 158	5062
					3785
					3791
					5041
					7F_6

^a Photographic method.
^b Doublet.

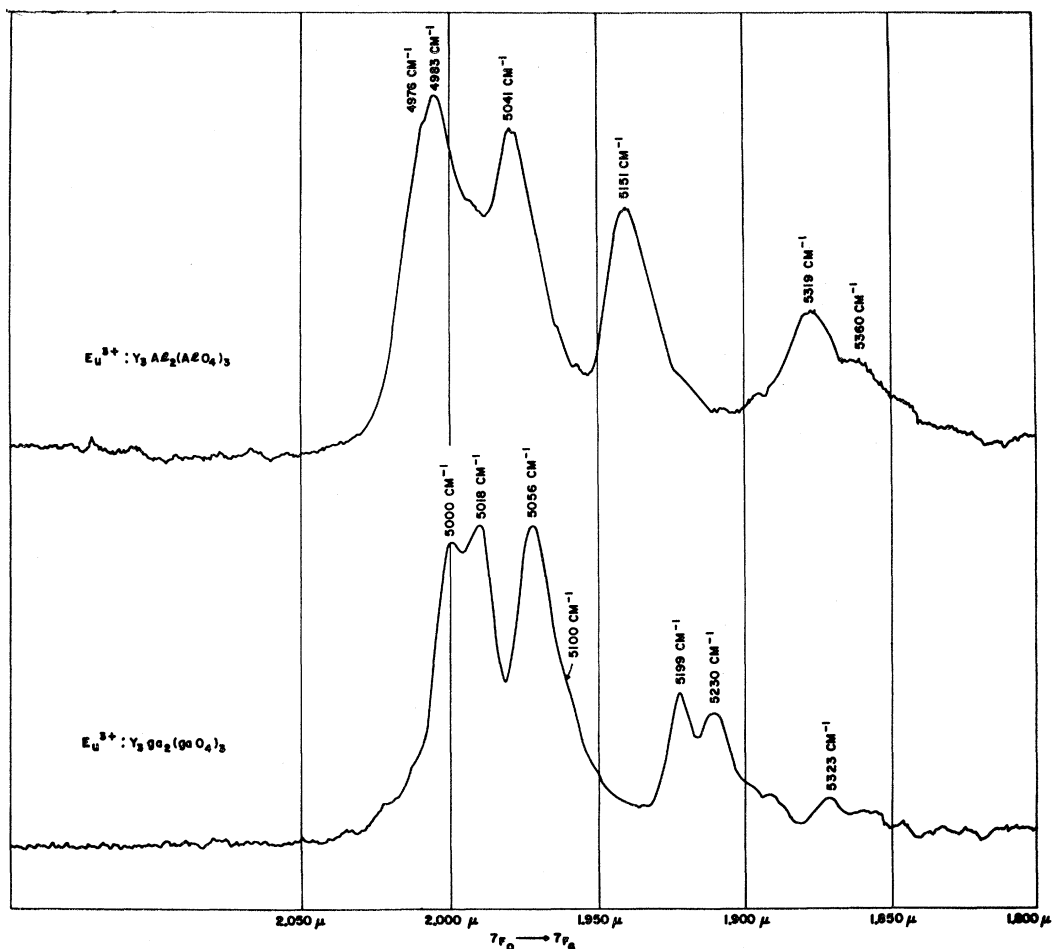


Fig. 4. The absorption spectrum of $\text{Eu}^{3+}:\text{YAIG}$ and $\text{Eu}^{3+}:\text{YGaG}$ between 2.05 and 1.80 μ at 30°K.

a. Absorption Spectrum in the Visible

At 300°K a complicated spectrum has been recorded in the region between 4830 and 4950 Å. At liquid helium temperature this spectrum consists of three bands, all showing fine structure. Peaks occur at 4840.0, 4843.5, 4854.0, 4857.0, and 4867.0 Å. They represent transitions from the ground state to crystal field levels within the 5D_4 manifold. These absorption bands are given in Table IV.

b. Absorption Spectrum in the Infrared

Groups of absorptions have been observed in $\text{Tb}^{3+}:\text{YAIG}$ between 2000 and 5900 cm^{-1} .

The absorption spectrum between 2130–2614 cm^{-1} ; 3365–3725 cm^{-1} , and 4397–4710 cm^{-1} consist of transitions which originate in the ground level and terminate on Stark levels of the 7F_5 , 7F_4 , and 7F_3 manifolds of $\text{Tb}^{3+}:\text{YAIG}$. Absorptions at 5010, 5611, and 5633 cm^{-1} are due to transitions which originate in the ground level and terminate on levels of the 7F_2 and 7F_1 manifolds. The level of the 7F_0 state of $\text{Tb}^{3+}:\text{YAIG}$ has been estab-

lished at 5882 cm^{-1} above the ground level. The absorption spectrum of $\text{Tb}^{3+}:\text{YAIG}$ in the spectral regions of 2.5–2.1 μ and 2.05–1.65 μ is shown in Figs. 5 and 6. The spectrum of the terbium ion in the host-lattice yttrium gallium garnet in the same spectral regions is

TABLE IV. Absorptions of $\text{Tb}^{3+}:\text{YAIG}$ in the visible.

300°K (Å)	4.2°K (Å)
4838	4840 (20 661 cm^{-1})
	4843.5 (20 646 cm^{-1})
4855.3	4854.0 (20 601 cm^{-1})
	4857.0 (20 587 cm^{-1})
4867.3	4867.0 (20 546 cm^{-1})
4871.2	...
4873.8	...
4881.7	...
4887.8	...
4908.7	...
4920.0	...
4926.0	...
4932.0	...
4942.5	...
4947.5	...

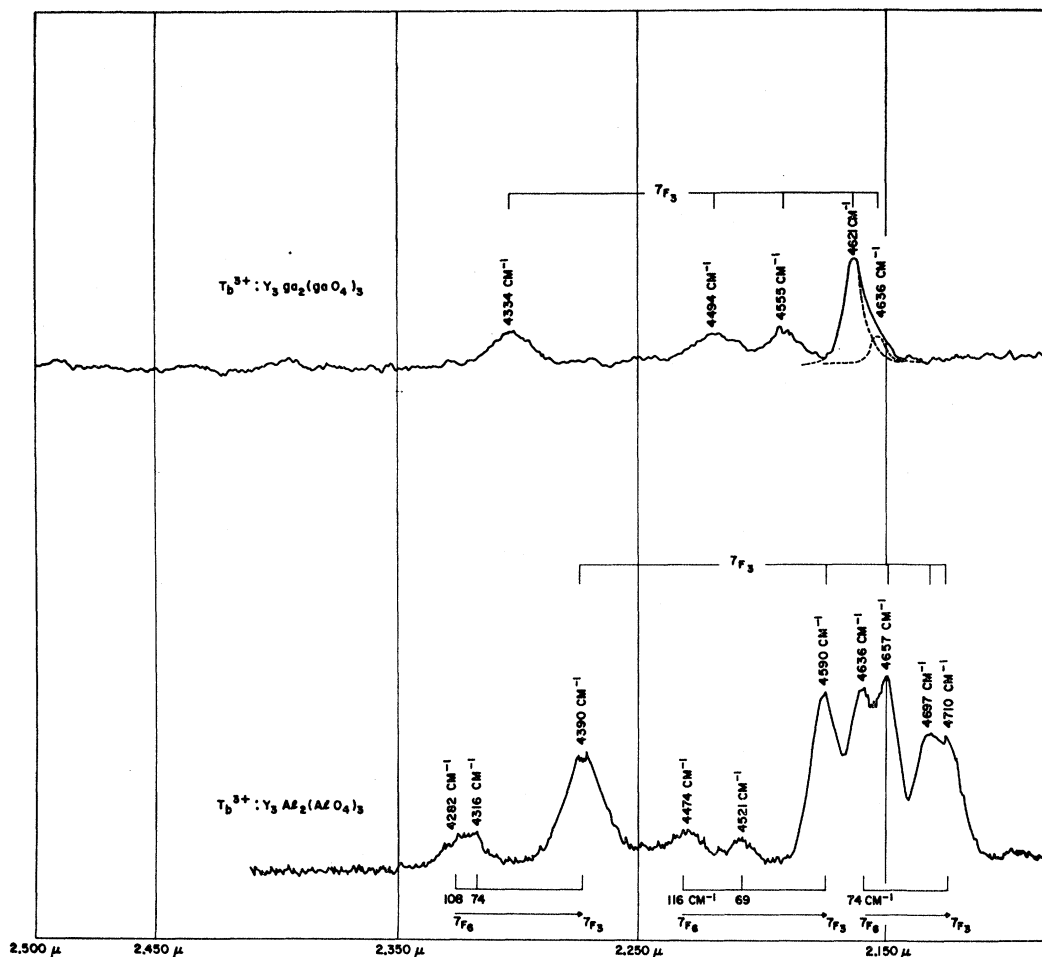


Fig. 5. The absorption spectrum of Tb^{3+} :YAIG and Tb^{3+} :YGaG between 2.1 and 2.5 μ at 30°K. Transitions in excited levels of the 7F_6 manifold are also indicated.

also shown. These absorption spectra were measured at 30°K. At this temperature some of the excited levels are still populated. Temperature dependence of the bands in the spectral regions as shown in Figs. 5 and 6 allows us to identify absorptions which originate in some of the Stark levels of the 7F_6 manifold. In Tb^{3+} :YAIG, levels are at $74 \pm 4 \text{ cm}^{-1}$, $122 \pm 4 \text{ cm}^{-1}$ above the ground level; in Tb^{3+} :YGaG a level has been found which is at $46 \pm 3 \text{ cm}^{-1}$ above the ground level. The positions of the absorption bands of Tb^{3+} :YAIG are given in Table V.

4. Fluorescence Spectrum of Tb^{3+} : YAIG

The fluorescence spectrum has been recorded photoelectrically in the region between 4840 and 6320 Å. A large number of lines have been observed. Additional detailed spectral information was obtained from photographic measurements at 4.2 and 1.8°K, which were made available to us by Dr. D. L. Wood of this laboratory. All data are shown in Table VI.

The fluorescence spectrum at 1.8°K indicates the presence of a level of the 5D_4 manifold at $\sim 20\,516 \text{ cm}^{-1}$ above the ground state. Transitions to this level have not been observed in the absorption spectrum in the visible at 4.2°K.

III. ENERGY LEVEL DIAGRAM OF Eu^{3+} : YAIG AND Tb^{3+} : YAIG

The energy level diagram of Eu^{3+} :YAIG and Tb^{3+} :YAIG has been inferred from both the absorption and fluorescence spectra. The positions of the energy levels of these ions are given in Table VII.

IV. ANALYSIS OF THE SPECTRUM OF Eu^{3+} : YAIG AND Tb^{3+} : YAIG

Our experimental results indicate that the $(2J+1=3)$ -fold degeneracy of the 7F_1 manifolds of both ions is completely removed by the crystal field. It is obvious that the symmetry of the crystal field is low. Since we are interested in the position of the Stark components

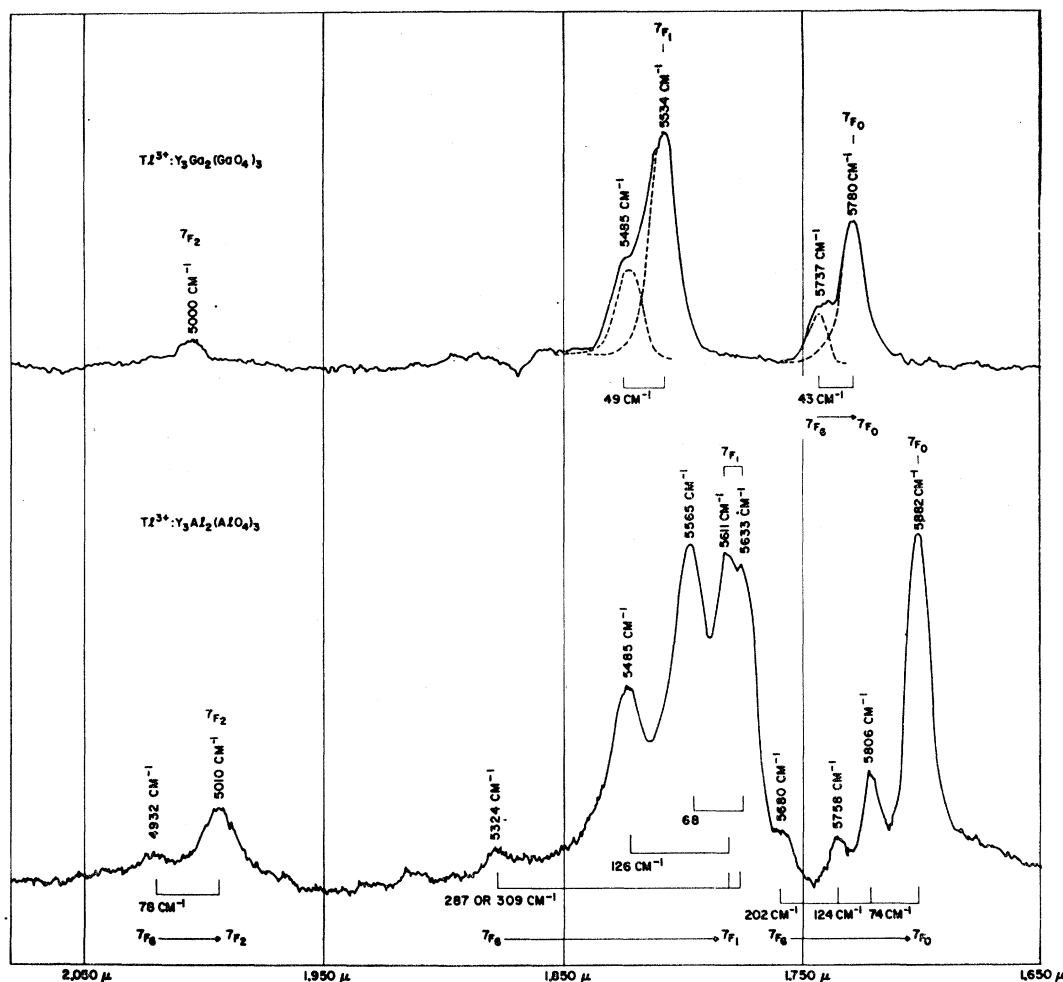


FIG. 6. The absorption spectrum of Tb^{3+} :YAlG and Tb^{3+} :YGaG between 2.05 and 1.65 μ at 30°K. Transitions originating in excited levels of the 7F_6 manifold and terminating on levels of 7F_2 , 7F_1 , and 7F_0 manifolds are indicated.

TABLE V. The absorption spectrum of Tb^{3+} :YAlG between 2130–5882 cm^{-1} . All transitions originate in the ground level.

Obs absorptions (cm^{-1})	Intensity ^a	Assignment
2130	st	7F_5
2140	st	
2191	st	
2478	st	
2600	w	
2614	w	7F_4
3365	st	
3380	st	
3413	st	
3488	st	
3605	st	
3697	m	
3725	st	7F_3
4397	m	
4590	m	
4650	m	
4697	m	
4710	m	
5010	w	
5611	m	7F_1
5633	st	7F_0
5882	st	

^a w = weak; m = medium; st = strong.

of the J manifolds relative to their unsplit positions, it is only necessary to consider the contribution to the Hamiltonian which is produced by the crystalline electric field.

The crystal-field perturbation is usually⁷ expanded in terms of the spherical harmonics:

$$V(r_k, \theta_k, \varphi_k) = \sum_n \sum_m \sum_k B_n^m r_k^n Y_n^m(\theta_k, \varphi_k), \quad (1)$$

where

B_n^m are constants,

$Y_n^m(\theta_k, \varphi_k)$ are spherical harmonics,

$n=6$ for 4f electrons.

The constants B_n^m depend on the positions of the neighbors around the rare earth ion. Although these positions are not known for the rare-earth ions in the host-lattice YAlG, such data are available for the iron garnet.¹¹ The yttrium ions which are replaced by the rare-earth ions, occupy orthorhombic sites of the cubic

¹¹ G. Z. Menzer, *Kristallografiya* 69, 300 (1929).

Table VI. Fluorescence of Tb^{3+} :YAlG. Fluorescence originates in levels of the 5D_4 manifold.

Obs (cm^{-1})	Series I 20 657- $\bar{\nu}$ 20 646- $\bar{\nu}$	Obs (cm^{-1})	Series II 20 601- $\bar{\nu}$ 20 589- $\bar{\nu}$	Obs (cm^{-1})	Series III 20 549- $\bar{\nu}$	Obs (cm^{-1})	Series IV 20 513- $\bar{\nu}$ Average	Assignment
		20 530	71	20 487	62	20 453	60	7F_6
						20 443	70	
						20 304	207	
20 371	275	20 328	271			20 247	266	
20 215	431					20 080	433	
		20 145	444	20 100	449	20 072	441	
				18 420	2129	18 389	2124	7F_5
				18 410	2139	18 378	2135	
18 483	2163	18 440	2161			18 354	2159	
						18 325	2188	
		18 255	2334			18 178	2335	7F_4
18 305	2352	18 235	2354			18 167	2346	7F_3
						18 048	2387	
		17 985	2064	17 947	2602	17 917	2596	
				17 935	2614	17 906	2607	
17 287	3359					17 148	3365	
17 258	3388	17 203	3387	17 167	3382	17 124	3389	7F_2
						17 092	3421	
						17 022	3491	
		16 988	3601	16 942	3607	16 911	3602	
16 239	4407	16 884	3717	16 831	3718	16 801	3712	
16 119	4538			16 163	4386			7F_1
				16 017	4532			
				15 972	4577			
		15 913	4688	15 867	4682			
15 939	4707			15 842	4707			
						15 067	5446	7F_0
15 045	5612	14 987	5614			14 900	5613	
15 026	5613	14 966	5634	14 922	5627			
14 770	5880	14 728	5873	14 668	5881			

* Levels of 7F manifolds not observed in the absorption spectrum in infrared

space group $O_h(10)Ia3d$. Eight oxygen ions located on the corners of a distorted cube are the closest neighbors. The B_n^m 's in the iron garnet have been calculated by Dillon and Walker.⁸ Their calculation shows that B_2^0 , B_2^2 , B_4^0 , B_4^4 , B_6^0 , and B_6^4 are the most important terms. Recent crystal-field calculations on the splitting of J manifolds of Nd^{3+} :YAlG indicate⁶ that the symmetry of the crystal field is approximately tetragonal. By employing the operator equivalent method of Stevens, Elliott, and Judd,¹²⁻¹⁴ we can write the crystal-field Hamiltonian H_c as

$$H_c = \alpha[A_2^0 Y_2^0 + A_2^2(Y_2^{+2} + Y_2^{-2})] \\ + \beta[A_4^0 Y_4^0 + A_4^4(Y_4^{+4} + Y_4^{-4})] \\ + \gamma[A_6^0 Y_6^0 + A_6^4(Y_6^4 + Y_6^{-4})], \quad (1a)$$

where α , β , γ are operator equivalent constants and

$$A_n^m = \langle r^n \rangle B_n^m \quad \text{with} \quad (r^n) = R(r)^2 r^{n+2} dr.$$

It has been shown that some of the J states of the trivalent rare-earth ions depart quite drastically from Russell-Saunders coupling. These deviations are, however, small for the 7F states of the Eu^{3+} and Tb^{3+} .¹⁵

The splitting of the 7F_1 manifold is directly related to the parameters A_2^0 and A_2^2 . The position of the Stark

components of this manifold as a function of the ratio A_2^2/A_2^0 is shown in Figure 7. Values of these parameters for Eu^{3+} :YAlG calculated for the three possible assignments, which are indicated with a , b , and c in Fig. 7, are given in Table VIII. From absorption and fluorescence spectra we have been able to establish the levels of the 7F_1 manifold of Eu^{3+} : $\text{Y}_3\text{Ga}_2(\text{GaO}_4)_3$ ¹⁶ at 307, 345, and 388 cm^{-1} above the ground level. The parameters A_2^0 and A_2^2 calculated from these data, using the assignments corresponding to those for Eu^{3+} :YAlG, are also given in Table VIII.

It is straightforward to show that the crystal field parameters A_2^0 , A_4^0 , A_4^4 , A_6^0 , and A_6^4 do not completely remove the $(2J+1)$ -fold degeneracy of manifolds with integral values of J . Independent of the values of these crystal-field parameters one expects one doubly degenerate level for $J=1$ and $J=2$; two doubly degenerate levels for $J=3$ and $J=4$; and three doubly degenerate Stark components of $J=5$ and $J=6$ manifolds. Either the parameters A_2^2 , A_4^2 , and A_6^2 or J mixing can remove this degeneracy. Our experimental results indicate that some of the Stark components of Eu^{3+} and Tb^{3+} :YAlG and also of Eu^{3+} :YGaG are close together (Table VII). The number of these doublets agree with the number of doubly degenerate Stark levels of the 7F manifolds in a field of tetragonal symmetry. The

¹² K. W. H. Stevens, Proc. Phys. Soc. (London) **A65**, 209 (1952).

¹³ R. J. Elliott and K. W. H. Stevens, Proc. Roy. Soc. (London) **A218**, 553 (1953).

¹⁴ B. R. Judd, Proc. Roy. Soc. (London) **A227**, 552 (1955).

¹⁵ G. S. Ofelt, J. Chem. Phys. **38**, 2171 (1963).

¹⁶ A complete analysis of the spectrum of Eu^{3+} :YGaG is discussed in the following paper [J. A. Koningstein and J. E. Geusic, Phys. Rev. **135**, A726 (1964)].

TABLE VII. Energy levels of Eu^{3+} and Tb^{3+} :YAIG.

Levels of Eu^{3+} :YAIG (cm ⁻¹)	Assignment	Number of Stark levels	Levels of Tb^{3+} :YAIG (cm ⁻¹)	Assignment	Number of Stark levels
0	7F_0	1	0	7F_6	9
286	7F_1	3	5	7F_5	9
307			61		
455	7F_2	4	70	7F_4	7
819			116		
902			207		
1010			270		
1022	7F_3	7	432	7F_3	6
1358			443		
1832			2128		
1842			2138		
1915			2161		
1959			2189		
2000			2335		
2008	2350				
2221	2387				
2856	7F_4	6	2601	7F_5	5
2865			2612		
2957			3364		
3137			3383		
3147			3417		
3248			3489		
3787	7F_5	5	3603	7F_6	8
3791			3697		
3946			3721		
4097 ^a			4394		
4226 ^a			4535		
4976	7F_6	8	4577	7F_2	1
4983			4590		
5028			4682		
5062			4707		
5151			5010		
5319			5446		
5358			5612		
5445			5632		
17 220	5D_0	1	5882	7F_0	1
18 952	5D_1	2	20 513	5D_4	6
18 991			20 548		
21 356	5D_2	3	20 588	5D_3	4
21 448			20 601		
21 473			20 546		
24 639	5D_3	4	20 659	5D_4	6
24 678			20 513		
24 683			20 548		
24 697			20 588		

^a Split in Eu^{3+} : $\text{YGa}_2(\text{GaO}_4)_3$.

observed splitting of the doublets indicates a small deviation from tetragonal symmetry. This deviation in the gallium garnet is larger than in the aluminum garnet, which implies that the parameters A_2^2 , A_4^2 , and A_6^2 are larger in the gallium garnet than in the aluminum garnet. As a result, we conclude that assignment *a* in Fig. 7 is the correct one for Eu^{3+} :YAIG.

The doublet-doublet spacing of the Stark components

TABLE VIII. Values of A_2^0 and A_2^2 for Eu^{3+} :YAIG and Eu^{3+} :YGaG.

Assignment ^a (cm ⁻¹)	Eu^{3+} :YAIG	Eu^{3+} :YGaG
(a) A_2^0	265	103.5
A_2^2	± 52.5	± 95
(b) A_2^0	-282	-135
A_2^2	± 370	± 107.3
(c) A_2^0	-248	-71.1
A_2^2	± 422	± 203

^a For Eu^{3+} :YAIG, see Fig. 7.

of the 7F_3 , 7F_4 , and 7F_5 manifolds of Eu^{3+} and Tb^{3+} :YAIG have been employed to evaluate values of the crystal field parameters A_4^0 , A_4^4 , A_6^0 , and A_6^4 , neglecting the terms A_4^2 and A_6^2 for these ions. A comparison of observed and calculated splitting of the 7F manifolds of both ions can be seen in Figs. 8 and 9. Values of the parameters which were used to calculate the splittings are given in Table IX.

Discrepancies between calculated and observed splittings are most pronounced for those Stark components

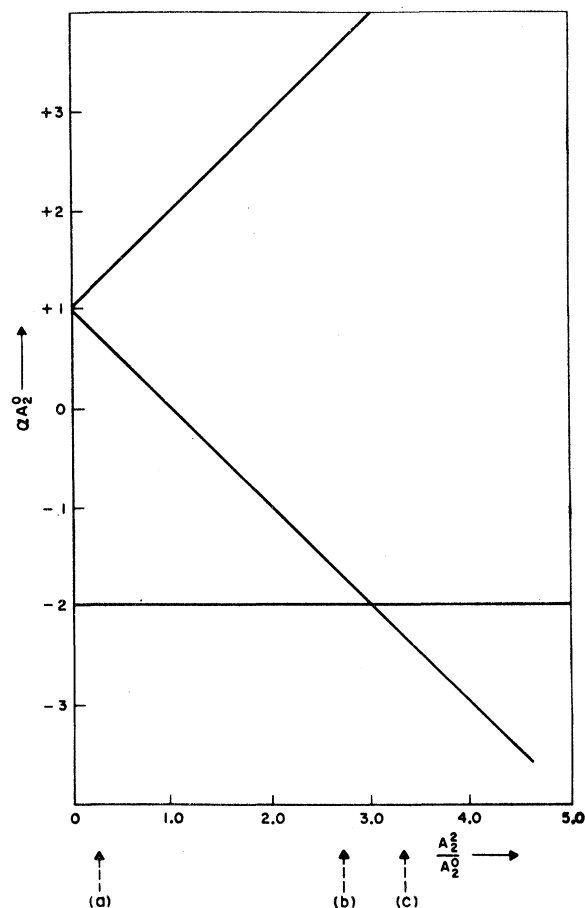


FIG. 7. The splitting of a $J=1$ manifold as a function of the ratio A_2^2/A_2^0 . *a*, *b* and *c* refer to the assignments possible for the 7F_1 manifold levels of Eu^{3+} :YAIG.

TABLE IX. The values of the crystal-field parameters $A_n^m = \langle r^n \rangle B_n^m$ for Eu^{3+} and Tb^{3+} in YAIG in cm^{-1} .

	A_2^0	A_2^2	A_4^0	A_4^4	A_6^0	A_6^4
$\text{Eu}^{3+}:\text{YAIG}$	268	51	-190	950	94	-1150
$\text{Tb}^{3+}:\text{YAIG}$	266	50	-184	920	93	-1115

which are far removed from the center of gravity of the J manifolds. These discrepancies are probably due to J mixing. The disagreement between calculated and observed splitting is greatest for the 7F_6 state; such a disagreement was found by Judd for Eu^{3+} ethylsulfate.¹⁷

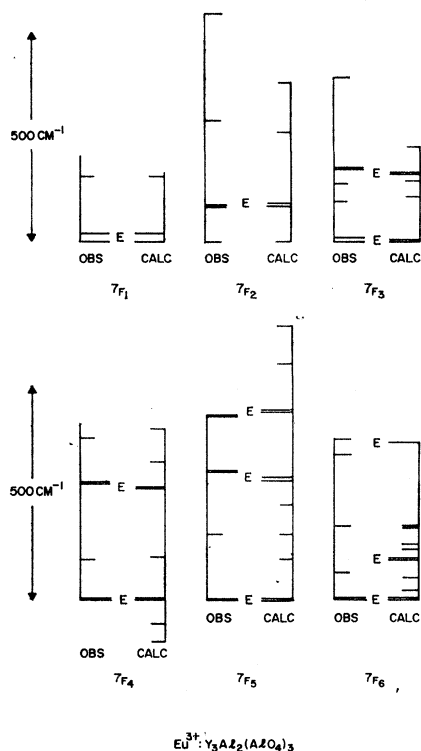


FIG. 8. Calculated and observed splitting of 7F manifolds of $\text{Eu}^{3+}:\text{YAIG}$. E stands for the doublets and indicate in general the deviation of tetragonal symmetry.

¹⁷ B. R. Judd, *Mol. Phys.* **2**, 4, 407 (1960).

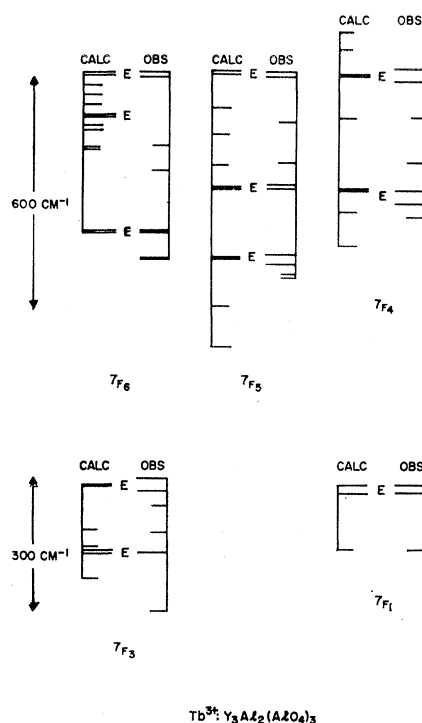


FIG. 9. Observed and calculated splittings of the 7F manifolds of $\text{Tb}^{3+}:\text{YAIG}$. E stands for the doublets.

It should also be noted that the observed doublet spacing is larger than the calculated spacing. This is probably due to the fact that the parameters A_4^2 and A_6^2 are ignored in the calculations.

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